

## FLOW-FIELD OF A 12-LOBE CONVOLUTED MIXER

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#### **Abstract**

The flow-field of a fuel/air mixing system with an axisymmetric lobed mixer was numerically investigated. Large-scale streamwise vortices are formed immediately downstream of the trailing edge, stretched further downstream, and finally broken into fragments where more intense mixing occurs. numerical and experimental results indicate that the length required for streamwise vortices breakdown in the confined flow-field of an axisymmetric lobed mixer is much shorter than that of planar lobed mixers subject to parallel For the configuration and freestreams. conditions studied, the streamwise vortices start to breakdown at three wavelengths downstream of the mixer trailing edge.

#### 1 Introduction

Lobed mixers have been applied to a number of engineering applications, such as jet noise reduction, infrared suppression and improvement of propulsion efficiency for gas turbine engines. More recently, they have emerged as an attractive method for enhancing fuel/air mixing in advanced combustion systems to reduce pollutant formation and to improve efficiency.

The underlying physics of planar lobed mixers in parallel freestreams has been extensively studied by a number of researchers [1-8]. They have pointed out that the counterrotating pairs of streamwise vortices generated by lobed mixers play a key role in mixing enhancement, where the interfacial surface area between two streams and the local gradients of

flow properties are increased. Werle et al. [1] found that the streamwise vortices experience a process, formation. i.e., intensification and breakdown, and more intense mixing occurs in the third region. Eckerle et al. [3] confirmed the above observation and pointed out that the length required for the flow to reach the third step was a function of the velocity ratio across the mixer. The evolution of streamwise vortices was further studied by Yu [9] in a low-speed wind tunnel at a freestream velocity ratio of 1:1. It was found that there was no vortex breakdown within seven wavelengths downstream of the mixer trailing edge three for trailing edge configurations.

In addition to the large-scale streamwise vortices, vorticity components or transverse vortices parallel to the trailing edge are also present in the flow-field when the freestream velocities on either side of the lobe are not equal. These relatively small-scale transverse vortices associated with the instability of the shear layers between the two streams can further intensify the mixing process [4,5]. Moreover, there are also horseshoe vortices formed around the front of the lobes. However, the strength of these vortices is an order of magnitude less than either streamwise or transverse vortices and has little impact on the overall mixing process [8].

Lobed mixers with geometrical configurations similar to the turbofan engine exhaust section were intensively studied in 1970s and 1980s. To date, it is still an active research subject aiming at design optimisation of lobed mixers or ejectors to improve engine performance and noise reduction [10-11]. Among the significant findings of these studies

is that the lobed mixer can generate streamwise vortices more efficiently (i.e., less pressure drop) than the conventional methods [12].

In contrast, studies of lobed mixers relevant to practical combustion systems are rare. With flow visualisation of a passive scalar, Belovich et al. [12] explored the mixing enhancement of three lobed mixers in an axisymmetric coaxial jet. Recently, Hu et al. [13] measured instantaneous & averaged velocities and inferred vorticity maps in an axisymmetric lobed jet flow with a 3-D PIV system. However, these investigations were carried out in open flows where the conditions are benign to advanced laser diagnostics.

In this paper, the confined flow-field of an axisymmetric 12-lobe convoluted mixer is numerically studied. The geometrical set-up of the mixing system is pertinent to many combustion designs using advanced lean premixing concepts and gaseous fuels [14]. The objective of the present work is to understand the flow features and mixing augmentation mechanisms of the lobed mixer in the axisymmetric confined flow. The numerical results compared with the limited experimental data obtained from a 2-D PIV system.

#### 2 Experimental Measurement

Figure 1 schematically shows a portion of the experimental set-up used for the fuel/air mixing research at the Gas Turbine Environmental Research Centre. More detailed information of the experimental facility and instrumentation are available in reference [14]. The mixer/fuel spoke section, immediately downstream of the contraction section of the inlet conditioning chamber, is 177.8 mm long and 50.8 mm in diameter. It hosts a 12-lobe convoluted mixer attached to the enlarged section of the central fuel pipe. The lobed mixer has a wavelength ( $\lambda$ ) of 9.69 mm, lobe height (h) of 14.5 mm and wall thickness of 1 The inward and outward penetration angles ( $\alpha$ ) are 22.6° following a 15 mm long straight splitter. There are six fuel spokes

welded to the enlarged end of the fuel pipe and the outside diameter of spokes is 3.175 mm. Since the objective of the present work is to study the flow features and the fuel volume flow rate is only a few percent of that of air, the fuel flow was neglected in the numerical simulation and turned off during the PIV measurement.

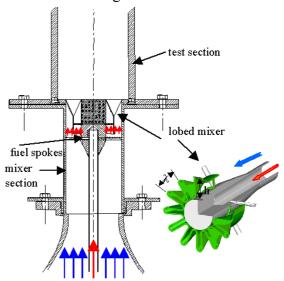


Figure 1 Schematic of the experimental set-up

Downstream of the mixer/fuel spoke section is the test section. It is 381 mm long, and has a square cross-section of 52×52 mm and a 50.8 mm circular exit at the downstream end. The corners of the cross-section are rounded with a radius of 10.2 mm. An exhaust chamber is connected to the test section exit and the flow is drawn out by an extraction fan.

PIV velocity measurements were carried out at an airflow rate of 1.580 N m<sup>3</sup>/min. The corresponding Reynolds number was  $3.8 \times 10^4$ based on the mixer diameter and  $7.6 \times 10^3$ according to the wavelength of the lobed mixer. Double-pulsed laser generated by twin Nd:YAG lasers from NewWave Corp. was used to form a light sheet through the test section. To achieve this, an optical transmission set-up was arranged and the resultant thickness of the laser sheet was about 1 mm. A high resolution CCD camera with 1280×1024 pixels (FLOWMASTER3 from LaVision ) was aligned orthogonal to the laser sheet and a narrow-band filter at 532 nm was mounted in front of a collection lens to minimize background noise. To synchronize

operations of the camera and laser, a programmable timing unit was employed. time interval of 6 - 15 us between pulsed laser pairs was used to provide an average pixel displacement of 2. The region of interest covered a quadrant of the test cross-section with a camera resolution of 0.027 mm/pixel. Al<sub>2</sub>O<sub>3</sub> particles with a nominal size of ~1 µm were used to seed the flow. Image acquisition and processing were all done by a PC equipped with the LaVision system. Two-dimensional velocity vectors were then calculated using the second-order standard cross-correlation and an adaptive window shifting with a final interrogation window size of  $16 \times 16$  pixels. At a given cross-section, sixty instantaneous image pairs were taken at a frequency of 4Hz to provide the mean flow field.

#### 3 Numerical Simulation

Three dimensional, steady, turbulent, isothermal flows were considered, and a commercial software package, Fluent, was used for the simulations in the present study.

#### 3.1 Computational Domain

The computational domain covered the mixer/fuel spoke section and the test section. Figure 2 shows the middle portion of these two sections. One quarter of the flow-field was considered due to the symmetry in geometry and a hybrid hex/ted mesh was generated over the computational domain.

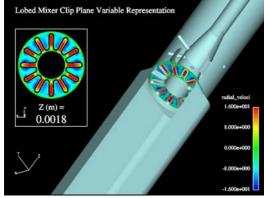


Figure 2 The middle portion of the computational domain

Figure 3 shows the mesh of the top portion of the mixer/fuel spoke section. To resolve the flow details, fine meshes were generated around the lobed mixer, fuel spokes and the upstream portion of the test section. Hex or prism layers were generated at all wall boundaries to properly account for the wall boundary effect and the y<sup>+</sup> values were maintained in a range Volume mesh adaption was from 1 to 5. performed to reduce rapid variation of cell volumes and to improve numerical accuracy and convergence speed. The total number of cells was 1.66 million. To check grid independence of the numerical solutions, another mesh was created using both velocity gradient and volume adaption and the total number of cells reached 2.05 million. The difference in numerical solutions obtained from these two meshes was negligibly small.

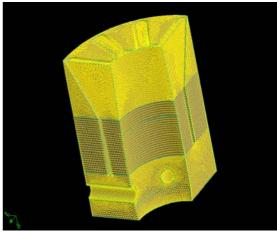


Figure 3 Mesh of the top portion of the mixer/fuel spoke section

# **3.2 Boundary Conditions and Physical Models**

The PIV measured velocity profile and turbulence intensity were imposed at the air inlet of the mixer/fuel spoke section. The discrepancy of the airflow rate calculated from the velocity profile was less than 2% in comparison with the metered value. A hydraulic diameter of 38.1 mm and a room temperature of 293 K were also assigned at the air inlet. At the exit of the test section, atmospheric pressure was defined.

The re-normalization group (RNG) k-e turbulence model was used to model turbulence in the flow. It is considered that the model is capable of accounting for the effects of flow swirling and rapid straining and has shown substantial improvements over the standard k-e model [15,16]. At the walls, an enhanced wall boundary treatment was applied, where an enhanced two-layer model is combined with enhanced wall functions and the viscous sublayer and fully turbulent regions are smoothly blended.

#### 3.3 Solution Methods

A segregated solver with second-order accurate schemes was used to resolve the flow-field. The normalized residual was less than  $1.7 \times 10^{-5}$  for velocity components, and  $5 \times 10^{-5}$  for turbulent kinetic energy and dissipation rate. For the continuity equation, the residual reached  $8 \times 10^{-4}$  normalized by the largest absolute residual in the first five iterations. The computations were performed on a dual, 1 GHz Pentium III processor unit with 2GB of RAM memory.

#### 3.4 Flow Patterns and Velocity Contours

Figure 4 illustrates the variation of axial velocities at cross-sections  $z/\lambda = 0.2$  to 4 downstream of the mixer trailing edge. Two recirculation zones (negative axial velocities) are observed due to the sudden expansion of the flow passage. One is behind the bluff body of the fuel supply in the centre region of the flowfield and the other is at the corner of the square cross-section of the test section (see Figs. 1-2). The magnitude and gradient of the axial velocity decrease rapidly downstream of the mixer due to the enhanced turbulent mixing. shows the contours of radial velocities at the same cross-sections as in Figure 4. Note that at  $z/\lambda = 0.2$  and 1, large outward (positive) radial velocities occur in the outward lobe regions, while large inward (negative) radial velocities are observed in the inward lobe regions. Flow moving in the opposite directions forced by the convoluted mixer generates large-scale streamwsie vortices and greatly enhances the mixing process. As in the case of axial velocity, the radial velocity magnitude and gradient decrease rapidly away from the mixer trailing edge.

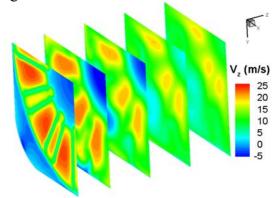


Figure 4 Axial velocity distributions at  $z/\lambda = 0.2, 1, 2, 3$  and 4

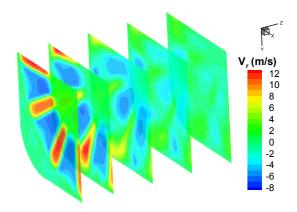


Figure 5 Radial velocity distributions at  $z/\lambda = 0.2, 1, 2, 3$  and 4

#### 3.5 Streamwise Vortex Development

Figure 6(a) shows the velocity vectors at the cross-section,  $z/\lambda = 0.2$ . Flow motions towards and away from the centre of symmetry are clearly observed in the inward and outward lobe regions, respectively. Figure 6(b) presents a vorticity contour plot of the resulting streamwise vortices for the same cross-section. Superimposed on the vorticity plot is the trailing edge contour of the lobed mixer. Three counterrotating pairs of ribbon vortices are formed immediately downstream of the mixer trailing edge. Note that the magnitudes of these vortices are large and their gradients are steep. In addition to streamwise vortices, counter-rotating pairs of horseshoe vortices wrapping around

each inward and outward lobe peaks are also predicted. In the present study, transverse vortices are not considered since the upstream flow velocity is the same on either side of the mixer and the effect of these vortices on the flow-field is believed insignificant [4,5,8].

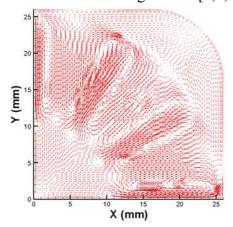


Figure 6(a) Vector plot at  $z/\lambda = 0.2$ 

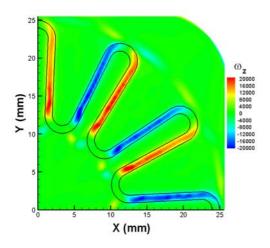


Figure 6(b) Streamwise vorticity at  $z/\lambda = 0.2$ 

Figure 7 gives the vector and streamwise vorticity plots at  $z/\lambda = 1.5$ , the six ribbon vortices become wider and distorted. As expected, a pair of counter-rotating vortices is formed at the corner of the test section due to the corner effect. Further downstream of the mixer, as shown in Fig. 8 for section  $z/\lambda = 3.0$ , the six vortices are starting to breakdown into fragments, and the flow-field becomes more complicated than that in the case of planar lobed mixers subject to parallel freestreams. The pair of corner vortices becomes stronger at this cross-section.

Figures 6 - 8 illustrate the formation, stretch/expansion, and breakdown of streamwise vortices generated by the 12-lobe convoluted mixer. As mentioned earlier, Yu [9] studied the development of streamwise vortices of three types of planar lobed mixers in a low-speed wind tunnel. The lobe wavelength and height of the three mixers were 33 mm, the penetration angle was 22° and the freestream velocity ratio was one. It was found that no vortex breakdown within was observed seven wavelengths downstream of the mixer trailing edge for all three configurations. One of the important findings from the present study is that the breakdown of the streamwise vortices in the confined flow-field of an axisymmetric lobed mixer is much earlier than those observed in planar lobed mixers. This information is important for the design of mixing ducts to ultimately reduce combustor length.

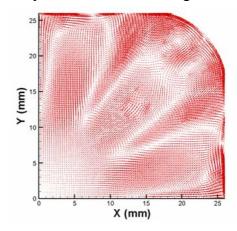


Figure 7(a) Vector plot at  $z/\lambda = 1.5$ 

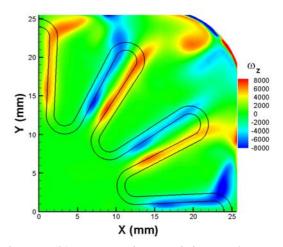


Figure 7(b) Streamwise vorticity at  $z/\lambda = 1.5$ 

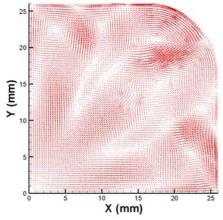


Figure 8(a) Vector plot at  $z/\lambda = 3.0$ 

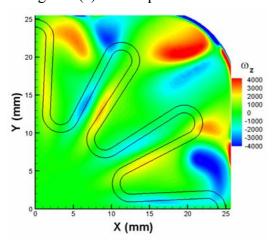


Figure 8(b) Streamwise vorticity at  $z/\lambda = 3.0$ 

#### 4 Comparison with Experimental Results

As mentioned earlier, the velocity distributions at a number of horizontal cross-sections were measured by the PIV system and the streamwise vorticity distributions were then inferred. Figures 9 - 11 show the streamwise vorticity contours at cross-sections  $z/\lambda = 0.8$ , 1.5 and 3.0 with a view window of  $20.5 \times 21.5$  mm. Similar to the numerical results, the strength of vortices decreases with an increase in distance downstream of the lobed mixer trailing edge. Three counter-rotating pairs of streamwise vortices are clearly observed at sections  $z/\lambda =$ 0.8 and 1.5. At section  $z/\lambda = 3.0$ , the counterrotating vortices are starting to intersect with each other and their shapes are no longer well defined, which implies the vortex breakdown occurs. This is consistent with the numerical

observations. Like the numerical simulation, a pair of counter-rotating vortices is also observed at the corner of the square cross-section for  $z/\lambda = 0.8$ , 1.5 and 3.0, and the strength increases with an increase in downstream distance.

It is noted that the vorticity magnitudes of the numerical results are larger than the corresponding experimental values (Figs. 7-8, Difference in spatial resolution, deficiencies of numerical physical models and measurement uncertainties may contribute to this observed discrepancy. To some extent, averaging over and between the interrogation windows was assumed in the PIV measurement, which tended to smooth gradients of flow properties. Deficiencies of the current turbulence models were observed in the previous combustor simulation [16]. It should be mentioned that the direct comparison of vorticity between experimental and numerical results regarding lobed mixers has not been seen before in author's knowledge.

Moreover, another discrepancy between the prediction and measurements is the flow rotating in the streamwise direction within the central recirculation zone. This experimentally observed (Figs. 9-11), but it is not shown in the numerical results (Figs. 6-8). This may attribute to that the flow in the recirculation zone is highly unsteady. In the numerical simulation, the mean velocity was averaged over an infinite time, while in the PIV measurements, only sixty instantaneous images were assembled. All these discrepancies will be further addressed in the future.

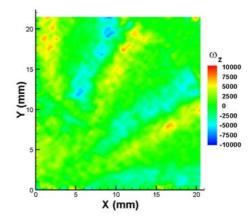


Figure 9 Streamwise vorticity at  $z/\lambda = 0.8$ 

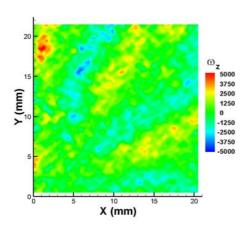


Figure 10 Streamwise vorticity at  $z/\lambda = 1.5$ 

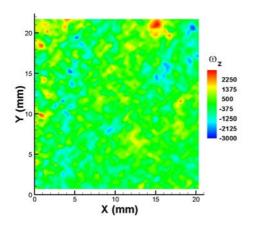


Figure 11 Streamwise vorticity at  $z/\lambda = 3.0$ 

### 5 Summary

The confined flow-field of an axisymmetric lobed mixer in a fuel/air mixing system relevant to practical low emission combustion designs was simulated. The numerical solutions were qualitatively compared with the PIV experimental results. The streamwise vortices experience a three-step process, i.e., formation, stretch and breakdown. This process in the confined flow of the axisymmetric lobed mixer accelerated. significantly For configuration and conditions considered, the streamwise vortices start to breakdown three wavelengths downstream of the mixer trailing edge, which agrees with the experimental measurements.

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