

A BLUNTED CONE IN A SUPERSONIC HIGH-ENTHALPY NONEQUILIBRIUM UNDEREXPANDED AIR JET

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Heat flux, pressure, catalysis

Abstract

A calculation and experimental study was conducted with the flow, heat flux and pressure distributions over the front and side surfaces of a blunt cone in a non-equilibrium high-enthalpy ($h_0 = 25$ MJ/kg) supersonic ($M = 4$) air flow. Experiments were performed in a VAT-104 wind tunnel (WT), TsAGI. The nose part of the model with a small-radius nose $R_w = 10$ mm and half angle $\theta = 10^\circ$ was inside the "Mach cone" of the underexpanded jet flowing out from the WT nozzle. Numerical and experimental results are in agreement.

1. Introduction

Simulation of thermo-chemical interaction between high-enthalpy flows of air and other gases and heat-protective materials (HPM) in high-enthalpy wind tunnels (WTs) for flight conditions of bodies with hypersonic speeds in atmosphere of the Earth, Mars, and other planets is among key problems of air thermo-dynamics [1].

Inductive (electrodeless) plasmatorches which produce high-enthalpy chemically pure gas flows, have a good potentiality in such simulation, particularly in respect to the thermal effect of heterogeneous catalytic reactions of atomic recombination [2-15]. Such WTs are utilized, in particular, to carry out ground experimental researches of the thermal protection for the flight conditions of hypersonic aircraft (HA) in the upper regions of the Earth atmosphere (about 60 – 100 km). These WTs enable to study HPM properties such as surface catalyticity, emissivity, thermal stability in flows of various gases. Such works

have been performed for many years with inductive plasmatorches in TsAGI (VAT-104 WT), IPMech RAS (IPG-4), TsNIIMASh, Von-Karman Institute, etc.

To analyze the experimental data, in particular, the catalytic properties of modern HTMs, and to transfer them in full-scale conditions of the hypersonic flight of bodies in the atmosphere, it is necessary to know in detail the flows realized in the experiment, as well as the physical processes taking place in the WT and on model surfaces. To solve these and other challenges of modern aerodynamic experiments, one should simulate numerically the supersonic flows of chemically reacting gases and heat exchange for specific experimental conditions, including those implemented in the VAT-104 WT, TsAGI [10]. Today, there is a serious gap between high-level mathematical and physical models applied in hypersonic aerodynamics and approximate models utilized for the analysis of WT flows. Numerical simulation for subsonic and supersonic regimes was successfully fulfilled.

In a number of cases, flows in WTs are more complicated in respect to the analysis of obtained experimental data than the hypersonic flows near bodies incoming into the atmosphere. The wind-tunnel gas heated in the heater up to high temperature cools down when the flow speed rises as the flow goes out through the nozzle into the working chamber. The gas temperature rises again behind the shock wave induced by the body. At the same time, in the flight, the gas reaches high values only after passing the shock wave induced by the body. Consequently, the gas properties near the model in the WT and near the HA surface in the flight may differ significantly at the same values of

stagnation enthalpy and pressure on the body surface.

The technology of calculation of such flows is based on a software system of numerical integration of Navier-Stokes equations and special programs-generators which include data bases for thermodynamic and transfer properties of individual gaseous substances (HIGHTEMP) created in the Institute of Mechanics MSU [5].

In the present paper, numerical investigation was done for the processes and flows in a chemically non-equilibrium model of the gas medium, in the heater and channel of VAT-104 WT, TsAGI, for the air dynamics of flowing-out underexpanded high-enthalpy air jets and for the model tested in the experiments; the results are compared with the experiment.

The aim of this work was to determine the heat flux and pressure distribution over the front and side surfaces of the blunt cone in the non-equilibrium high-enthalpy ($h_0 = 25$ MJ/kg) supersonic ($M = 4$) air flow. Experimental investigations were carried out in the VAT-104 TsAGI. The front part of the model with a small-radius nose $R_w = 10$ mm and half angle $\theta = 10^\circ$ was inside the "Mach cone" of the underexpanded jet flowing out from the WT nozzle. It is known that the disturbances occurring in the working chamber of the hypersonic WT cannot penetrate into the area inside the "Mach cone" (toward the nose part of the model): this fact facilitates interpretation of the test results in comparison with the experiments in subsonic wind tunnels.

In order to measure the heat flux distribution, heat-capacity heat-flux probes were utilized (copper inserts thermally insulated from the model body). These probes were calibrated by a standard technique on a special calibrating heat-flux facility ETGU, TsAGI.

To measure the pressure distribution, pressure gages were used; they were located directly inside the model. It allowed significant reducing of the pressure measurement duration in the flow by means of utilization of short routes from the receiving orifice to the pressure gage. Short duration of the measurement (test) provided complete and repetitive safety of the

model under the conditions of a strong action of the heat flux on it.

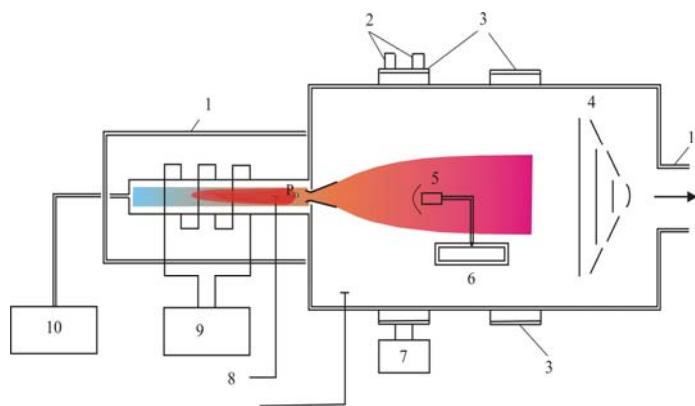
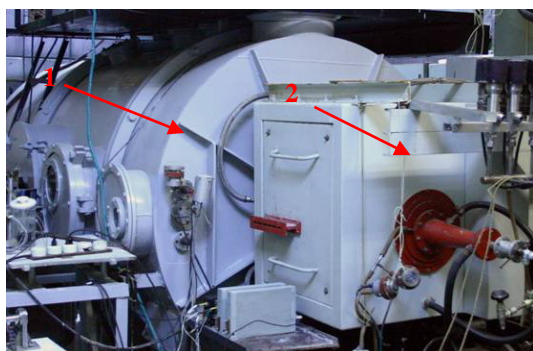
A special high-speed mechanism of model introduction into the high-enthalpy flow was developed for the short-run test in the WT (the time of jet crossing is below 0.2 s).

2. Experimental equipment

2.1 VAT-104 wind tunnel

The basic elements of the wind tunnel VAT-104 are the gas heater, nozzle, working chamber, and a system of pumping-out with a vacuum capacity, figure 1. Figure 1b shows the basic schematic of the VAT-104 WT.

The gas is heated with a high-frequency inductive heater, which permits to have a spectrally pure high-enthalpy gas flow. The heaters of this type feature high stability and repetitive accuracy of enthalpy, total stagnation pressure, and heat flux from one test to another (the parameter deviations from assigned values do not exceed 3%). The inductor is fed from the high-frequency (HF) generator VChI-4-160/1.76. The generator is of a two-loop configuration, with controlled feedback. The generator power in the anode circuit is up to $W_a = 240$ kW, the oscillating power is up to $W_{\sim} = 160$ kW, and the frequency is $\nu = 1.76$ MHz. Standard discharge ignition is carried out in an argon medium as the discharge chamber is vacuumed to the pressure $P_0 = 5 - 30$ Pa. Then the working gas is supplied, its flow rate and heater power are increased smoothly. The flow rate of the working gas is controlled by a throttle system, manually or automatically (a program sets the mode). The mode onset time is from 10 to 30 seconds. Various gases such as nitrogen, air, argon, argon-oxygen mixture, etc. can be used as the working substance. This time, air was used. The plasmatorch heats the working gas up to the temperature of $T_0 = 5,000 - 8,000^\circ\text{C}$, (the stagnation enthalpy is $i_0 = 10 - 40$ MJ/kg) as its flow rate is up to $G = 4$ g/s and the total pressure is up to $P_0 = 50$ kPa (0.5 bar). The main parameters of the heater



a). Photograph
1-working chamber, 2- high-frequency (HF) inductive heater

b). The basic schematic
1 - induction heater, 2 - CCD camera, 3 - optical windows, 4 - cooler, 5 - model, 6 - input mechanism, 7 - AGA thermo vision, 8 - pressure gauges, 9 - HF generator, 10 - gas supply, 11 - to the vacuum system

Fig. 1. VAT-104 WT

operation in the VAT-104 WT are studied by contact and optical diagnostic techniques. It is found that the vibration and rotational temperatures in the settling chamber coincide within the experimental error limits (10%).

– The results of heat flux measurements made with calorimeters and sensors with coatings of extremely high and extremely low catalytic activity enabled to establish that as the anode voltage was $U = 8.5 - 10.5$ kV and the pressure in the heater was $P_0 = (10 - 40)$ kPa, air dissociation degree is $\alpha = 0.5 - 0.9$;

With the lower heater power, lower flow parameters can be realized: the pressure of $P_0 = 3 - 6$ kPa, $i_0 = 10 - 20$ MJ/kg, $\alpha = 0.1 - 0.3$.

The working cell is an Eiffel chamber. It is a cylinder with a diameter of 1.6 m and a length of 4 m. The inductive heater with a water-cooled nozzle is connected to the front end face of the working chamber. The back end face is connected to the vacuum capacity via a vacuum lock.

Inside the working cell, there is a fast-acting mechanism of model introduction into the flow and a heat exchanger which cools down the high-temperature gas jet after the model is immersed in flow. The model was introduced into the flow when the assigned

stationary flow mode was reached in the wind tunnel, Fig. 2.

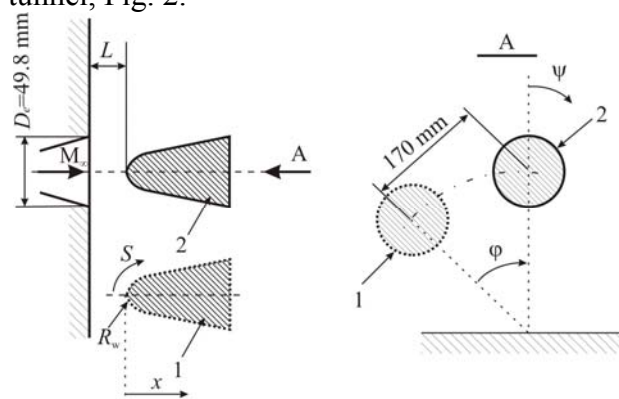


Fig. 2. Fast-acting input mechanism.
1 - before model introduction into the jet,
2 - after model introduction

In this experimental research, the Laval nozzle was utilized; it had the throat radius $R^* = 7.2$ mm, the outlet section radius $R_e = 26.4$ mm, and the half angle in the supersonic part of 15° . The pressure in the working part of VAT-104 may vary from 1 to 1,000 Pa, depending on the quantity and type of involved pumps and gas flow rates. In these experiments, the jet flowing out from the nozzle of VAT-104 is underexpanded. Mach numbers $M = 4 - 8$ can be reached in the jet at various distances from the nozzle exit.

The maximum duration of the test in VAT-104 is limited by the possibility of working chamber cooling; it varies from 20 minutes as the pressure in the settling chamber is $P_0 \approx 50$ kPa to two hours at $P_0 \approx 5$ kPa. The heat flux to the cold wall ($T_w = 18$ °C) at the stagnation point of the flat end face of the streamwise-aligned cylinder with a radius of $R = 35$ mm is $q_0 = 100 - 1500$ kW/m².

Deviations of the enthalpy from one test to another normally do not exceed 3%. In repetitive tests, the error of heat flux determination is 5 – 10%.

2.2 Model

The methodical model purposed for the distribution of the heat flux density is made of stainless steel and has a shape of a blunt cone which is identical to the standard sample shape.

There are nine calorimetric heat-flux gages on the model; they are equipped with thermo-anisotropic bushings and a thermocouple to measure the temperature of their cold junction. The locations of the heat flux probes are shown on Fig. 3 and Table 1.

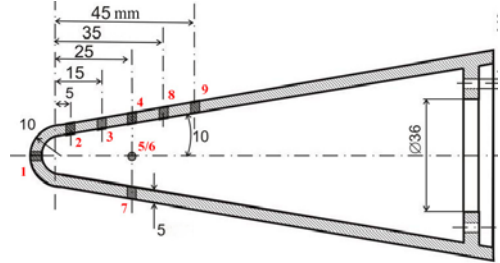


Fig. 3. Locations of the heat flux probes

The heat flux probe has a brass calorimeter shaped as a small cylinder, its diameter is 1.5 mm, and its length is 4 mm.

Table 1: Locations of the heat flux probes

Probe number	1	2	3	4	5	6	7	8	9
x , mm	0	15	25	35	35	35	35	45	55
S , mm	0.00	20.8	30.9	41.1	41.1	41.1	41.1	51.2	61.4
ψ , deg	0	0	0	0	270	90	180	0	0

of the cylinder (dot welding). All thermocouple cables are connected to the connector which is located in the aft body of the model.

A heat-insulating bushing, which presents a tight spiral of brass foil and a thin glass-cloth band, serves for thermal insulation of the calorimeter from the model walls. Spiral turns are glued with a high-temperature glue VK-21 (heat resistance up to 700 – 800°C). Owing to such a probe design, the temperature distribution by the cylinder depth and long turns of the brass foil are approximately similar (especially on the spiral

At the same time, the effective thermal conductivity across the spiral turns is not high because of the low thermal conductivity of the glass cloth and glue. It permits to linearize probe's characteristics and hence increase the potential measurement time up to 3 – 4 seconds. In order to sufficiently reduce leakages resulting from the plasma flow, the probes were coated with an insulator (thin, approximately 2 μ m layer of gel SiO₂). It

enabled us to illuminate discharge current to turns adjoining the calorimeter), Fig. 4.

Each heat-flux probe was graduated many times in the ITGU pulse thermal calibrating facility based at NIO-8 TsAGI. The facility permits to supply step-function signals q_0 of the convective heat flux with known magnitudes. The probe calibrating factor K_1 is determined by the response signal $U_0(\tau)$:

$$K_1 = q/(dU/d\tau)$$

Later, these calibrating factors will be utilized to determine the heat flux density during the tests of the model in the VAT-104 in the ITGU pulse thermal calibrating facility based at NIO-8 TsAGI $q = k \times (dU/d\tau)$, where $k = K_1 \times K_2$

Here U is the probe signal in millivolts recorded during tests, K_2 is the factor of the amplifier of the signals established in the VAT-104 WT.

The model for pressure distribution measurement was equipped with five small-scale inductive gages (type DMI-0.6-III) for the

rated range of 0.6 kgs/cm². The probes were preliminary mounted on a special unit installed

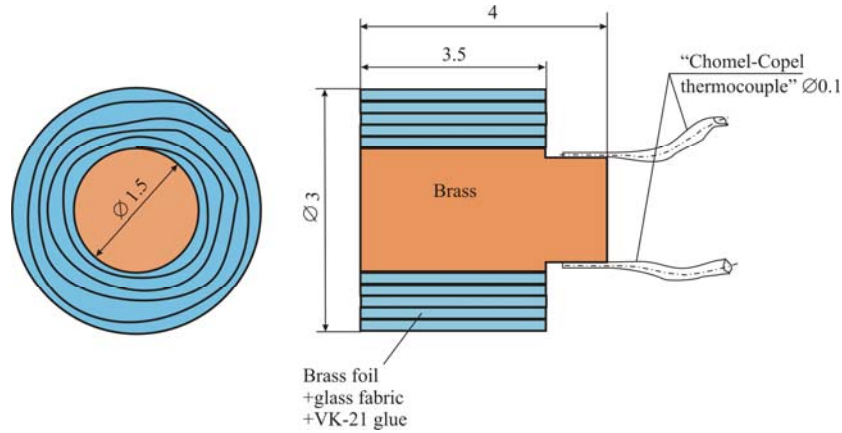


Fig. 4. Heat flux probe design

inside the model body. Fig. 5 presents the photo of the model with the probes inside.



Fig. 5. Model for pressure distribution measurement

The receiving orifices of the gages ($d_{in} = 1$ mm) lied on one line along the model generatrix. The coordinates of the pressure sampling points are listed in Table 2.

Table 2: Orifices locations

Probe number	1	2	3	4	5
x , mm	0	15	25	35	55
S , mm	0.00	20.8	30.9	41.1	61.4

The pedestal areas of the gages are connected with a sealed channel; this channel is a carrying collector for every gage, it has a special outlet tube, which connects the collector and the WT test section and also serves as a channel of bearing pressure supply for gage calibration. Electrical leads of the gages are unsoldered for the connector RS32 TV. The gages work together with the 8ANCh-23 amplifying apparatus on the carrier frequency.

The magnetic biasing frequency for the probes is 20 kHz.

The gage at $S = 0$ purposed for the measurement of the pressure in the stagnation point of the model has special thermal protection – a plug which presents a tangle of copper wire of 0.08 mm located in the channel of the receiving duct of the gage.

3. Results of numerical investigations of the flow around the model

The numerical simulation of the stationary laminar flow of the air plasma in the heater for experimental conditions in the WT VAT-104 TsAGI was performed on the base of full Navier-Stokes equations and simplified Maxwell equations for the time-averaged amplitude of the tangential component of the high-frequency electric field intensity $\vec{E}(t, x, r) = \vec{E}_\theta(x, r)e^{-i\omega t}$, written in the cylindrical system of coordinates, with due regard for the axial symmetry of the problem. Here $\omega = 2\pi f$ is the circular frequency. Plasma radiation was ignored. The electromagnetic field is a superposition of the induction coil field and annular plasma currents; it was treated as a monochromatic one, with the assigned frequency f which depends on the high-frequency current in the inductor. For the calculation, the real inductor was replaced by four infinitely thin ring turns.

The source terms (the Lorentz force and Joule heat release) involved in the Navier - Stokes equations were expressed via the tangential component of the complex amplitude of the curl electric field.

The calculation of the high-frequency electromagnetic field was conducted together with the calculation of the gas-dynamic equations on the base of the local-one approximation of the Maxwell equations. The followings assumptions were used:

- the plasma is quasi-neutral;
- the magnetic permeability of the plasma is $\mu = 1$;
- the dielectric permeability of the plasma does not depend on the electromagnetic field and hence does not depend on the coordinates;
- the bias current can be ignored;
- the variation of the electric field in the axial direction can be ignored as compared to its variation in the radial direction

$$\frac{\partial}{\partial x} E_{\theta} \ll \frac{\partial}{\partial r} E_{\theta}.$$

The latter assumption leads us to the locally one-dimensional approximation for the Maxwell equations, and it significantly simplifies the task. The corresponding equation for determining the tangential component of the curl electric field and boundary condition for

this equation are given in [4-5] where the flow of the equilibrium air plasma was considered.

During the combined calculation of the flow and electromagnetic field in the heater of VAT-104 WT, TsAGI, the power N_{pl} applied to the discharge was assigned as a governing parameter; the respective current in the inductor was determined during the solution process. In turn, the value of N_{pl} was found with the aid of the generator power N_{ap} measured experimentally, by the anode supply multiplied by the plasmatorch efficiency. At calculations sizes of the Laval nozzle were accepted slow differing from experimental values: the throat radius was $R^* = 7.5$ mm, the outlet section radius was $R_e = 25$ mm,

Fig. 6 present the calculated distributions of the static temperature and Mach number; the data illustrate the pattern of the flow around the blunt cone model at the static pressure of the flow in the output cross section of the nozzle; the pressure is somehow above the pressure in the WT test section.

At the same time, the ratio of the pressure on the model surface P_w to the total pressure P_0 decreases with increasing distance from the nozzle section exit to the stagnation point of the model $X_s = L$ (fig. 7 and 8).

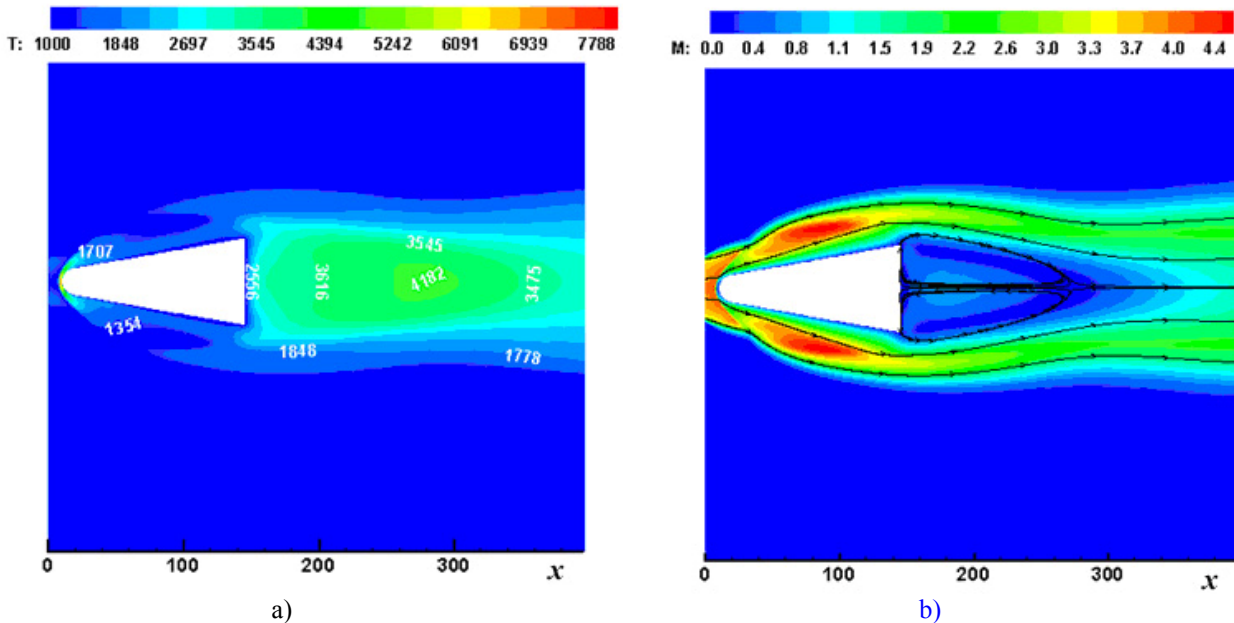


Fig. 6. Flow structure near the a blunt cone immersed in a supersonic flow
a) Static temperature, K; b) Mach Number

Specifically the pressure ratio in the stagnation point $S = 0$ (stagnation pressure) P_s to the total pressure P_0 is changed sufficiently.

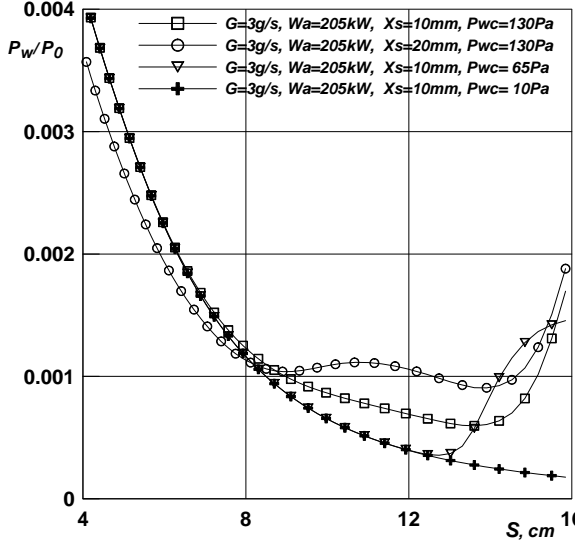


Fig. 7. Dependences of the ratio of the pressure at the cone surface to the total pressure P_w/P_0 for various pressure values in the working chamber

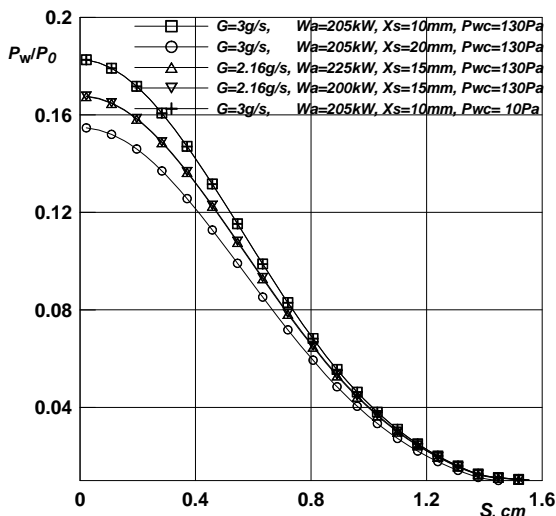


Fig. 8. Dependences of the ratio of the pressure at the nose part of the model to the total pressure P_w/P_0 for various parameters.

Experimental investigation of the heat flux and pressure distributions

The experiment sequence was the following: the model was installed on a holder fastened into a fast-acting mechanism of model introduction in the flow. Before being introduced into the flow, the model axis was parallel to the nozzle axis and 160 mm far from

it, the stagnation point of the model was at the distance of $X=10$ mm from the nozzle exit section.

Then the WT test section was sealed and pumped out. As the pressure of 1 – 100 Pa was reached, the plasmatorch generator was actuated. The discharge was ignited, and smooth mode onset was carried out via increased anode power of the heater W_a and air pressure ahead of the throttle (pressure in the settling chamber P_{fk}). The duration of the mode onset was about 50 – 80 s. As the necessary parameters (W_a and P_{fk}) were reached, the operator introduced the model in the flow. The heater was switched off in 2 – 3 s after introducing the model in the flow. (the pressure in the settling chamber P_{fk} practically does not differ from total pressure P_0), the heater power was $W_a = 190$ kW, and the air flow rate was $G = 2.5$ g/s.

As an example, let us consider the results of one of the tests at the pressure in the settling chamber was $P_{fk} = 355$ torr.

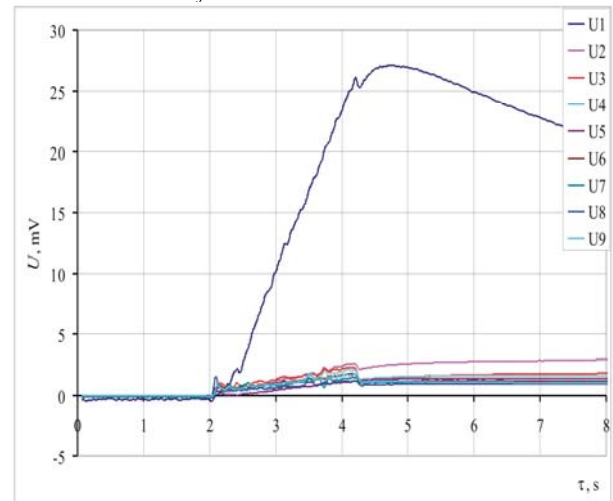


Fig. 9. $U_i = f(\tau)$

It follows from Fig. 10 that the experimental findings and numerical data of the heat flux are in qualitatively agreement.

In order to determine the pressure distribution, four tests were carried out at various pressures in the settling chamber and a constant heater power. Let us analyze the results of one test. The settling-chamber pressure was $P_{fk} = 350$ torr.

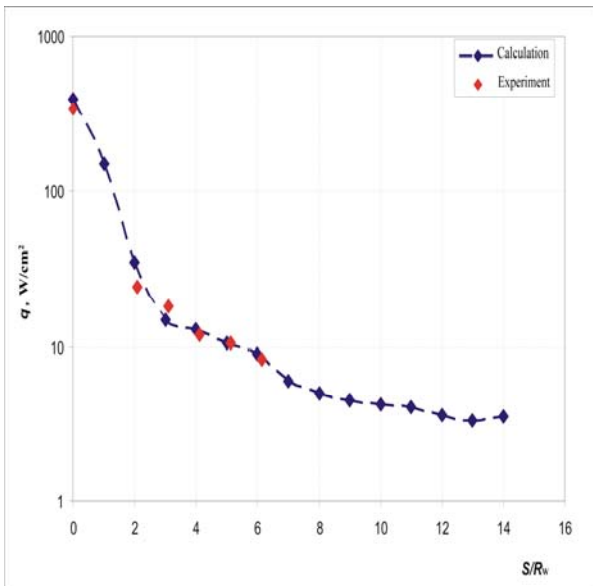


Fig. 10. Heat flux distribution over the model surface

Fig. 11 presents the comparison of the pressure distribution versus the distance to the stagnation point along the generating line. It is evident that the pressure obtained in the test is in qualitatively agreement with numerical results.

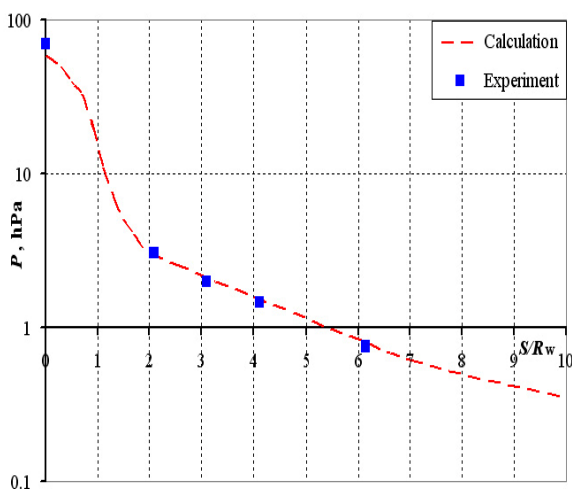


Fig. 11. Pressure distribution over the model surface

Conclusions

The numerical and experimental investigations were carried out to study the flow, heat flux distribution, and pressure distribution over the front and side surfaces of the blunt cone which was in a nonequilibrium high-enthalpy ($h_0 = 25$ MJ/kg) supersonic ($M = 4$) air flow. The tests were performed in the VAT-104 wind tunnel, TsAGI. The nose part of the model with a

small-radius nose $R_w = 10$ mm and half-angle $\theta = 10^\circ$ was inside the “Mach cone of the underexpanded jet flowing out from the WT nozzle.

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