# AN APPROACH TO PREDICTION FOR NATURALLY SHORT FATIGUE CRACK GROWTH BEHAVIOURS

V.Z.Jiang and B.Q.Xu
Beijing University of Aeronautics and Astronautics
Beijing, P.R.China

#### Abstract

A reasonable method for predicting naturally short fatigue crack growth(NSFCG) behaviours was proposed, good predictions relating to the actural experimental was achieved. This provided a better prospect in ultilizing NSFCG behaviours to damage tolarate design and life estimation of components.

### 1. Introduction

Considered that the process of fatigue damage of most engineering components in service conditions is acturally a process of NSFCG, which involved the crack growth under conditions of greatly diminished shielding effect[1], so the growth rates for short crack are found to be greater than those for long crack at the same apparent driving force[2]. Furthermore the rapid NSFCG rates are also confirmed at applied stress intensity levels well below the low R-ratio long crack threshold value. Consequentely, it is very impotant that the component design and life calculation based on damage tolerent design concepts must take the NSFCG behaviours[3] into consideration.

In this paper, a mothed for the prediction of NSFCG curves based on a reasonable inference was proposed, and its prediction ability was quite good.

### 2. Inference

It was suggested that the closure effect might play an important role in crack growth especially near the threshold regime. As Navarro's equation[4] was ultilized to describe the NSFCG process and it is pointed to be in the first grain, the threshold condition might be shown as

$$K_{th,int} = Y \sigma_{fl}(\pi D/2)^{1/2}$$
 (1)

in which a short crack growth is of almost no shielding effect, where K  $_{\rm th,int}$  is the intrisic threshold,  $\sigma_{\rm fl}$  is the fatigue limit, D is the average grain size, Y is the geometrical factor of stress intensity of short crack concerned.

On the other hand, in constant K max decreasing- $\Delta K$  test the growth rate of long crack would finally reach an effective threshold  $\Delta K_{th,int}$ , and in regime near the  $\Delta K_{th,int}$  the crack propagated also in the same situation of almost no shielding effect as mentioned above.

Therefore, considered that the K th.int might be equivalent the  $\Delta K$  th.eff and in the regime near the  $\Delta K$  th.eff of long crack growth curves there is surely a point in which the data equivalent to data of the velley point on the lower limit curve of NSFCG( at this time the initially short crack tip reaches approximately to the first grain boundary) at a certain applied stress.

Thus, a method for predicting NSFCG behaviours proceeded on the following way:

1. Take data(da/dN, $\Delta K$  eff) from a point near the  $\Delta K$ th.eff located on the curve obtained in constant K educated decreasing- $\Delta K$  test, and take it equivalent to the data(dc/dN, $\overline{K}$ ) of a velley point on the lower limit NSFCG curve at a certain applied stress, in which

Copyright © 1992 by ICAS and AIAA. All rights reserved.

$$\Delta K = Y \sigma (\pi D/2)^{1/2} \tag{2}$$

The corresponding applied stress level driving NSFCG consequentely can be given from equ. (2).

2. With the applied stress level given above, the ultimate tensile strength  $\sigma_u$ , the intrisic threshold Kth.int (= $\Delta K$ th.eff ) and the stress intensity  $\overline{k}$ , the critical demensionless crack size parameter  $n_e$  associated the minimal dc/dN at the velley point on lower limit curve in Navarro's equation can be calculated as

$$n_{e} = cos \left[ \frac{\pi}{2} \frac{\sigma}{\sigma_{u}} \left( 1 - \frac{\Delta K_{th,int}}{\overline{K}} \sqrt{n_{e}} \right) \right]$$
 (3)

3. At the same time, suppose the velley point rate dc/dN equivalent to the long crack growth rate da/dN selected and take c=D/2, then the factor f interprected as the fraction of dislocations on the slip band which participate in process of crack extension can be calculated by

$$f = da/dN / \left[ \frac{2(1-\nu)}{G} \sigma c \frac{\sqrt{1-n_c^2}}{n_c} \right] \eqno(4)$$

where G is the shear modulus, vis Poisson's ratio.

4. If data of three or more points are selected from the regime near the effective threshold and a least squares fit are performed, a relevant function between  $\sigma$  and f and a family of NSFCG curves  $\sigma$ -dc/dN-c can be predicted.

## 3. Verification

# Test material and its properties

300M steel was used as a test material, its chamical compositions (wt%): 0.39C, 0.91Cr, 1.12Ni, 0.63Mn, 0.4 Mo, 0.07N, 1.61Si. Heat treatment: austenitize 870°C, two tempers 300°C, prior austenite grain size D=0.025mm. Mechaical properties:  $\sigma_{\rm u} 2015{\rm MPa}$ ,  $\sigma_{\rm u} 21727{\rm MPa}$ ,  $\delta_{\rm s} 12.5\%$ ,  $\psi 52.9\%$ ,  $\sigma_{\rm -1} 853{\rm MPa}$ ,  $\Delta K$  th  $5.35{\rm MPa}\sqrt{m}$  (R=0.1).

### Constant K max decreasing-△K test

Fig.1 displays the results of constant Kmax decreasing-  $\Delta K$  test with Kmax=22.2MPa(m) and 11.1MPa(m). Since two curves all approach to the effective threshold( $\Delta K$  th.eff = 3.07MPa $\sqrt{m}$ ), the regime near  $\Delta K$ th.eff of two curves are close to each other, it provide convenience in taking data from these regimes.

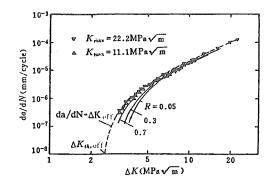


Fig.1 Long fatigue crack growth behaviours of 300M steel

# Predicting NSFCG behaviours

Three sets of pairs (da/dN, \( \Delta Kerr)\) were taken from data of

Table 1. Experimental and predicted parameters

selected long crack growth data		predicted corresponding NSFCG parameters		
da/dN(m/cycle)	ΔK <sub>eff</sub> (MPa√m)	σ(MPa)	n <sub>e</sub>	f
3.39*10-11	3.26	904.7	0.9991	0.0341
1.00*10-10	3.45	957.5	0.9965	0.0481
2.15*10 <sup>-10</sup>	3.62	1004.6	0.9962	0.0678

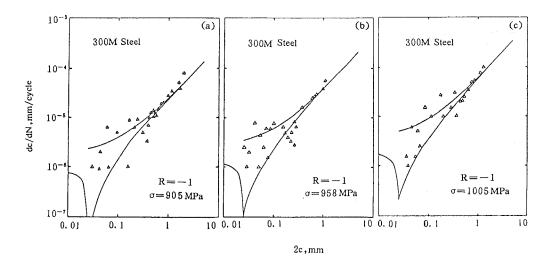


Fig. 2 Comparison of experimental NSFCG data of 300M steel with predicted upper and lower limit curves

near  $\Delta K_{\text{th.eff}}$  growth curve in constant  $K_{\text{max}}$  decreasing- $\Delta K$  test, corresponding NSFCG parameters calculated were listed in Table 1 and a power law expression such as

$$f=1.4921 \cdot 10^{-21} \sigma^{-6.5467}$$
 (5)

which represented a good relation between values of f and  $\sigma$  shown in Table 1.

Comparison between experimental and calculated results
Three sets of NSFCG test proceeded on stresses listed in Table 1, all experimental data(dc/dN,2c) were shown in Fig.2a,b,c respectively. The upper and lower limit curves derived by calculated parameters were shown in corresponding figures as well, in which the values of geome-

ponding figures as well, in which the values of geometrical factor Y determined by surface crack size parameter t/R and t/c (Fig.3) on the cylinder specimen[5], where t/c was taken as 0.8 approximately which agreed with

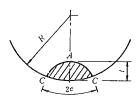


Fig.3 Surface crack size parameters of smooth cylinder specimen

the fractograph analysis, and curves predicted involved

most of experimental data obviously. For further verifing the prediction ability of this method a series of experimental life  $N_{\text{exp}}$  compared with corresponding predicted life  $N_{\text{pre}}$  were shown in Fig.4. the scatter factor covered

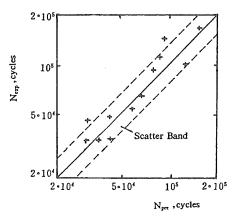


Fig.4 comparison of experimental life with predicted life of 300M steel

most experimental data were equal to 1.3 lower than the usual value of 2 or more, so the prediction ability was improved evidently.

### 4. Conclusion

It was supposed that the long crack growth behaviours near effective threshold in constant K max decreasing- $\Delta K$  test can be equivalent to the behaviours of naturally short fatigue crack which approach to the first grain boundary at a certain applied stress. As this was introduced in NSFCG equation developed by A.Navarro, the closure effect was considered and the NSFCG behaviours itselves were predicted also, so the procedure described above provides a good prospect in ultilizing NSFCG behaviours to damage tolarate design and life estimation of engineering structures and components.

#### Reference

- Ritchie R.O. and Yu W.(1986) Short crack effects in fatigue. A consequence of crack tip shielding. Small Fatigue cracks(Edited by Ritchie R.O. and Lankford J.), pp.167-189. Matell. Soc., London.
- Ritchie R.O. Yu W. Blom A.F. and Hom D.K. (1987) An analysis of crack tip shielding in aluminium alloy 2124: A comparison of large, small, through-thickness and surface fatigue cracks. Fatigue Fract. Engng Mater. Struct. 10, pp.343-362.
- Lankford J. and Hukak S.J. (1987) Relavance of the small crack problem to life-time prediction in gasturbines. Int. J. fatigue. 9, pp.87-93.
- 4. Navarro A. and de los Rios E.R. (1988) A microstructurally-short fatigue crack growth equation. Fatigue fract. Engng Mater. Struct. 11, pp.383-396.
- Murikami Y. (1986) Stress Intensity Factors Handbook, Vol.2, Comittee on Fract. Mech. The Society of Material Science, Japan. pp.662-663.