

ICAS-88-2.3.3 APPLICATION OF INTEGRATED FLUID-THERMAL-STRUCTURAL ANALYSIS METHODS

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Abstract

Hypersonic vehicles operate in a hostile aerothermal environment which has a significant impact on their aerothermostructural performance. Significant coupling occurs between the aerodynamic flow field, structural heat transfer, and structural response creating a multidisciplinary interaction. Interfacing state-of-the-art disciplinary analysis methods is not efficient, hence interdisciplinary methods integrated into a single aerothermostructural analyzer are needed. The NASA Langley Research Center is developing such methods in an analyzer called LIFTS, an acronym for Langley Integrated Fluid-Thermal-Structural analyzer. The evolution and status of LIFTS is reviewed and illustrated through applications.

Introduction

Design of lightweight structures and thermal protection systems for hypersonic vehicles depends on accurate prediction of the aerothermal loads, structural temperatures and their gradients, as well as structural deformations and stresses. Traditionally, an aerodynamicist predicts the surface pressure and heating rate assuming a rigid isothermal body. The aerodynamic heating rate is used by a structural heat transfer analyst to predict the structural temperature distributions. Finally, a structural analyst uses the temperature distributions and aerodynamic pressures to predict the structural deformations and stresses. Such a traditional independent approach requires several iterations between the different analysis methods and analysts. The approach is relatively inefficient because the incompatible mathematical models require extensive postprocessing to transfer data. Moreover, the interdisciplinary coupling and interactions, which are significant, are rarely addressed because the iterative process not only requires several additional solutions, but also remodeling in each analysis. An integrated multidisciplinary analysis procedure is required for accurate, timely prediction of the coupled response. The coupling occurs primary through the thermal response of the structure, because (1) the surface temperature

affects the external flow by changing the amount of energy absorbed by the structure, and (2) the temperature gradients in the structure result in structural deformations which alter the flow field and attendant surface pressures and heating rates.

To meet the analysis requirements for hypersonic vehicles the NASA Langley Research Center is developing an Integrated Fluid-Thermal-Structural (LIFTS) analyzer using finite element methods. The method is illustrated in Fig. 1 on an actively cooled structure. A general automated unstructured gridding is used to discretize the aerodynamic and coolant flow field and the structure for the thermal and structural analyses. Currently a single nonlinear finite-element algorithm provides the solution for the environment, loads, and response for all three disciplines. The flow field computational domain is adaptively refined based on flow field error indicators to minimize grid points and increase accuracy. Several graphic techniques are used to display the results.

This paper covers the historical development, status, and plans of the integrated finite-element fluid-thermal-structural methodology in LIFTS as graphically illustrated in Fig. 2. The development of a finite element thermal analyzer equivalent to standard finite difference thermal analyzers was initiated in the mid 1970's with the development of radiation, forced convection and conduction elements and interfaced with a structural analyzer (References are referred to in detail in the text.). The next step was the development of hierarchical thermal elements with nodeless variables and an integrated thermal-structural analyzer which eliminated the post processing interface. At this point the integrated thermal structural analyzer was interfaced with existing computational fluid dynamic analyzers and the development of an integrated fluid-thermal-structural analyzer initiated. Recent research has focused on the development of efficient algorithms, adaptive refinement techniques and a posteriori error estimates for the solution of the two and three dimensional Euler and Navier Stokes equations for the computational fluid dynamics portion of the integrated fluid-thermal-structural methodology. The latter effort led to the development of the Taylor-Galerkin algorithm which is applied in conservation form for all three disciplines in LIFTS. The algorithm development for the inherently nonlinear fluid equations led to unexpected benefits in the solution of nonlinear thermal and structural (plasticity and large deformations) behavior. Salient features of various problems are used to illustrate the benefits of

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certain approaches and to provide insight into methodology decisions.

Evolution of Integrated Fluid-Thermal-Structural Methodology

Interfaced Thermal-Structural Analysis

In the mid 1970's, NASA developed the airframe integrated supersonic combustion ramjet shown in Fig. 3. Tests demonstrated that the fixed geometry engine, which uses the airframe forebody as part of the inlet and the afterbody as part of the nozzle, could deliver positive thrust over a Mach 6 to 10 range. Standard disciplinary methods were used to independently determine the aerodynamic loads, the thermal response, and structural performance of the hydrogen cooled concept¹.

The surface pressure and heating rates were determined assuming a rigid isothermal body. These aerodynamic heating rates were used to predict the structural temperature distributions using a finite difference electrical analog procedure (MITAS²). Finally, the temperature distribution and aerodynamic pressures were used to predict the structural deformations and stresses using NASTRAN³. Even though thermal stresses and deformations were significant, the solution was not iterated to account for coupling between the flow field and the surface deformations and temperature⁴.

This thermal stress dominated problem emphasized the need for efficient methods of transferring temperature distributions to the structural model for the thermal stress analysis. The standard approach of interfacing two different codes was extremely inefficient⁵. Extensive postprocessing was required to interpolate and/or extrapolate temperature data from the thermal model to the structural model. Because of the different mathematical models and analysis methods, models with exactly the same nodal placement was impractical⁵. In fact, one of the greatest shortcomings in the thermal analysis was the lack of the automated model generation capability that existed for the finite element structural analysis⁶.

Existing finite element thermal analyzers were limited to conduction, convection to a known temperature, and radiation to space⁶. Hence, new finite element thermal methodology⁷⁻¹⁵ for mass transport, surface convection to an unknown temperature, and internal radiation¹³ were developed. The new elements developed for the thermal analysis of an actively cooled engine strut¹ are shown in Fig. 4. Several comparative studies demonstrated that the finite element procedure was equivalent or better than the finite difference lumped parameter approach⁷⁻¹⁵. One such example, shown in Fig. 5, compares the predicted aerodynamic skin temperature and coolant temperature along the engine strut. The initial comparison with approximately 3000 node MITAS and NASTRAN thermal models highlighted the benefits of the finite element model generation capability, which not only

reduced the time to construct a model but facilitated the verification of the model⁶. Current finite difference thermal analyzers do not have this severe shortcoming as finite element model generation capability has been exploited to construct thermal models. However, separate thermal and structural codes still require interfacing and interpolation of the temperature field to the structural model for the thermal stress analysis.

Even with finite element thermal and structural analyzers, an incompatibility remained⁷ between thermal and structural models as shown in Fig. 6. The thermal model of a section through the strut wall is shown on the left. The cooling jacket consists of an aerodynamic skin and fins with hydrogen as a coolant. This section is modelled with conduction, convection, and mass transport elements for the thermal analysis but is ignored in the stress analysis as the cooling jacket deforms plastically and adds negligible stiffness to the load carrying primary structure^{1,4,6,7}. The primary structure consists of the wall, modelled with a quadrilateral conduction/convection element and a rib modelled with a rod conduction/convection element. The primary structure has a thermal gradient along its length and through the thickness, which creates the thermal stress field. The optimal (minimum unknowns) thermal stress model, shown on the right, consists of a beam bending element and an axial member. The beam bending element requires the average wall temperature and through the wall temperature gradient, which are not generated by the thermal model. Hence, even with the same numerical methodology incompatibilities can exist between thermal and structural models. This incompatibility could be removed by compromising the structural model (increasing the number of unknowns) and using quadrilateral membrane elements with the same nodal locations as the thermal model.

Integrated Thermal-Structural Analysis

Compatibility between the thermal and structural models is not always achievable without severely compromising the efficiency of one or both of the solutions. For instance, a structural member that carries only an axial load could be modelled with a single finite element. However, if the member has an axial temperature gradient, several linear thermal elements may be required to accurately predict the temperature gradient in the element. If the structural model had the same nodal locations as the thermal model then the data transfer would be straight forward. However, the interior nodes would have to be constrained, so as not to act as hinges, for the structural analysis. These types of incompatibilities led to the development of hierarchical thermal elements with nodeless variables¹⁶⁻²⁰. Nodeless variables were used to obtain a higher order polynomial interpolation function without adding nodes—particularly nodes not required by the structural analysis.

The hierarchical integrated thermal-structural analysis method that evolved²⁰ is illustrated in Fig. 7. The example problem is a wing section with non-uniform heating (q) to the upper surface. The analysis approach,

shown on the right of the figure, is discussed below. A common discretization is used to suit the geometry, as shown in the upper left of the figure. The hierarchical thermal analysis initially assumes the temperature distribution to be linear producing the the bilinear result labelled $P_T = 1, 2$ FE (first order polynomial for element temperature distribution, two finite elements as shown on surface). An increase in the thermal polynomial to second order ($P_T = 2$) yields the nonlinear distribution labelled $P_T = 2, 2$ FE. A traditional analysis would have increased the number of linear finite elements to ten to achieve equivalent accuracy as shown ($P_T = 1, 10$ FE). The nodeless variable essentially floats so that one need not know or guess a priori the temperature distribution in order to locate elements. Hence increased accuracy is achieved without remodelling.

The next step in the hierarchical integrated thermal-structural analysis is the transfer of the thermal data to the structural analysis. This step is crucial and missing in interfaced analyses. That is, the conversion of the temperature field to equivalent thermal forces requires the same interpolation function used in the thermal analysis or, in other words, consistent thermal forces. If we ignored this step and transferred only nodal temperatures and then calculated the equivalent thermal forces with a linear interpolation function we would get a bilinear thermal stress distribution as shown by $P_S = 1, P_T = 1, 2$ FE. (For this analysis, bilinear, $P_S = 1$, structural elements were adequate.) However by using the appropriate interpolation functions the nonlinear stress field indicated by $P_S = 1, P_T = 2, 2$ FE is obtained. If the domain is modelled traditionally with ten linear elements ($P_S = 1, P_T = 1, 10$ FE) then the nonlinear stress distribution is obtained but prediction is only fair compared to the hierarchical prediction. The discontinuities occur at the nodes indicating a coarse grid.

Shuttle Flow-Thermal-Structural Analysis Experience

A major example of the difficulty in performing a complete flow-thermal-structural analysis without integrated methods was the Space Shuttle. The aerodynamicist provided pressure and heat transfer rates over the mission profile. The thermal analysis of the Shuttle was then performed using local three dimensional plug models⁵ as indicated by the solid areas in Fig. 8. Each thermal model, which consisted of approximately 200 degrees of freedom (dof), provided temperatures that had to be interpolated or smeared longitudinally and circumferentially to the structural nodal locations. Post flight evaluation of this procedure showed that the interpolation or smearing led to large discrepancies in the temperature levels and gradients, hence underprediction of the thermal stresses and deformations. One such evaluation²¹ used a complete cross section of the wing as shown in Fig. 9. A comparison in Fig. 10 of the interpolated temperatures and the results from a more detailed finite element thermal model illustrates the noted discrepancies.

In addition to the models being coarse, the complete load cycle for a given mission took approximately one calendar year. With this lengthy cycle, designs tended

to be frozen early and any modifications were also very costly. More efficient methods that could reduce the time to perform a load cycle analysis were obviously needed. The underlying goal of the integrated fluid-thermal-structural methodology is to reduce a load cycle calculation without compromising disciplinary results.

Integrated Fluid-Thermal-Structural Analysis

Fluid Algorithms and Adaptive Procedures

The next step was the addition of the fluid module to complete the desired integrated fluid-thermal-structural analysis methodology. Some investigators modified structural finite element algorithms for fluid analysis and concluded that finite element techniques were inferior to existing finite difference procedures²². The approach taken herein was to exploit all the finite difference technology in the development of new finite element algorithms for computational fluid dynamics²³⁻³⁰. This led to the on going development of several algorithms (See Fig 2.) such as the Taylor-Galerkin method of Morgan^{23,25} and the Petrov-Galerkin method of Hughes³¹.

The Taylor-Galerkin procedure is similar to a Lax-Wendroff finite difference algorithm. A Taylor series expansion is used to obtain recurrence relationships to march the solution in time. The Galerkin criteria is used to obtain the spatial discretization of the domain. Application of the Taylor-Galerkin algorithm to benchmark problems demonstrated accuracy and efficiency^{23,24,26,27}. Several of these problems required capturing shock waves and high thermal gradients near the surfaces. Since finite element thermal and structural methods traditionally used unstructured grids to transition from coarse to fine meshes in order to capture gradients, it was natural to consider unstructured meshes for the fluid domain. Although this was considered unorthodox by the finite difference community, adaptive unstructured methods were developed by Peraire and Morgan^{25,29} and Ramakrishnan, Bey, and Thornton³⁰ with great success. The adaptive remeshing procedure of Peraire et. al.^{25,29} uses only triangles and adapts the mesh based on error indicators of flow variables such as density and temperature. Ramakrishnan, et. al.³⁰ developed a mesh enhancement procedure using triangles to transition between coarse and fine quadrilateral meshes. They also used flow error indicators to adaptively enhance the mesh where required. Both procedures remove mesh points where unnecessary, hence obtaining near optimal meshes for the problem at hand.

The adaptive unstructured remeshing scheme of Peraire is illustrated in Fig. 11. The schlieren photograph on the left of Fig. 11 shows an incident oblique shock wave intersecting the bow shock wave of a cylinder immersed in a Mach 8 flow. This interaction results in a shock interference pattern, classified by Edney³² as a Type IV supersonic jet, that impinges on the cylinder surface. The final unstructured mesh adapted to the flow physics²⁷ is shown in the right of

Fig. 11. Note that the mesh density gradient simulates the flow density gradient given by the schlieren. The planar boundaries of the mesh encompass the flow domain and the circular part the cylinder. The solution is initiated on a relatively uniform mesh. The initial mesh and subsequent meshes are remeshed periodically (about three times) based on density error indicators until the solution converges. The lower part of Fig. 11 shows an enlargement of the shock front to illustrate that the element base is oriented parallel to the maximum gradient (perpendicular to the shock). The triangle dimensions are a function of the error indicators, which are a function of the gradient. Hence, if the second principle gradient is small the user can allow high aspect ratio elements (equality of error indicators in the principal directions) to decrease the problem size.

The shock wave interference problem illustrated above is a formidable thermal-structural design issue for hypersonic vehicles with airbreathing engines³⁴⁻³⁵. The incident shock is generated by the vehicle nose or compression ramps on the undersurface of the vehicle which acts to precompress the air flow passing into the engine as illustrated in Fig. 12. Aerodynamicist design for this shock-on-lip condition to maximize the compressed air flow into the engine and hence performance. The experimental configuration in the lower left of Fig. 12, which simulates the vehicle forebody and cowl leading edge, was used to define the aerothermal loads³⁴⁻³⁵. The schlieren photograph shows a supersonic jet interference pattern impinging on the surface of the cylinder. The interference pattern produces intense local amplification of the pressure and heat transfer in the vicinity of the jet impingement. The undisturbed (absence of incident shock) stagnation point pressure and heating rate can be amplified by factors from 6 to 30 depending on the shock strength and free stream Mach number³⁴⁻³⁵.

This experimental data was used to calibrate the finite element solution and adaptive meshing techniques. Both adaptive unstructured grid techniques performed well^{27,28,30}. However, the Taylor-Galerkin algorithm when applied to meshes with triangular and quadrilateral elements was found to be unstable at the transition nodes³⁰. A Runge-Kutta finite element algorithm proved effective for these meshes³⁰. The triangular remeshing procedure does not have the stability problems although it can have dispersion errors for large aspect ratio elements³⁰.

The severe gradients in the jet impingement region required extremely fine meshes to resolve the temperature gradient in the thermal boundary layer and hence obtain accurate heating rates²⁸. These small elements led to very small time steps to meet the stability requirements of the explicit algorithm^{30,36}. Although solutions could be obtained, they were impractical and led to the development by Thareja and Morgan²⁸ of an implicit finite-element cell-centered algorithm and the code LARCNESS, an acronym for Langley Adaptive Remeshing Code and NavEir Stokes Solver. LARCNESS results²⁸ are in good agreement with the Mach 8 experimental results of Wieting and Holden³⁴

as shown in Fig. 13. The local pressure (P) and heating rate (Q) distributions, normalized with respect to undisturbed flow stagnation point values, are shown on the right of Fig. 13. The undisturbed (no incident shock) distributions are also shown to emphasize the amplification of the loads. The adaptive unstructured computational mesh shown on the left of Fig. 13 required 8800 nodes, approximately 1/3 the amount required for a stretched but structured mesh³⁷. A layer of structured quadrilateral elements, which adapt circumferentially to the otherwise unstructured mesh, are used to capture the boundary layer. The uniformity was required in order to limit eigenvalues required in Roe's averaging technique²⁸. Mesh uniformity appears to also be required for current turbulent models, hence turbulence models need to be developed for unstructured meshes as they significantly reduce the computation effort.

Disciplinary Interactions

In all of the examples given, the flow field was coupled to the thermal response of the structure, since the wall temperature affects the amount of energy absorbed from the boundary layer. If the temperature distribution is known a priori then the flow field can be uncoupled from the thermal analysis by specifying the surface temperature distribution. An even stronger coupling occurs when the thermal or mechanical deformations of the structure alter the flow field making an otherwise uniform heating nonuniform or even creating local hot spots.

A metallic thermal protection system (TPS), which consists of 1'x1'x4" tiles mechanically fastened at the corners to a primary structure, glowing from aerodynamic heating (Fig. 14) illustrate this behavior³⁸. Prior to aerothermal exposure the TPS is flat. Exposure to the aerodynamic stream causes the tiles to thermally bow into the stream due to the in-depth thermal gradient. Each tile bows approximately spherically creating the quilt like surface shown in Fig. 14. Experimental data³⁹ and Navier-Stokes analyses⁴⁰ showed that the local maximum heating rate(q), equilibrium temperature (T_{eq}), and the total heat flux (Q) were increased above the flat surface value as shown in Fig. 15. The increase was a nonlinear function of the bowed height (h) to boundary layer thickness (δ_{fp}) ratio. In addition, as shown to the left of Fig. 15, the mechanism for the increased heating was a function of the tile alignment (longitudinal and diagonal) and was caused by flow impingement or compression on the protruding tile and vortices generated by the diagonally aligned array. This analysis was performed assuming an isothermal wall and a rigid spherical shape. Although both were reasonable assumptions for the objective of the study, the actual shape and temperature distribution are significantly different as implied by the resulting localized heat flux and temperatures which would alter both the indicated heating rate and the deformations⁴⁰.

This type of coupled flow-thermal-structural behavior obviously requires the integrated methodology discussed herein. The current capability in the Langley

Integrated Fluid-Thermal-Structural (LIFTS) analyzer, which uses the Taylor-Galerkin algorithm for all three disciplines, has been demonstrated for the two dimensional equivalent of the bowed TPS array⁴¹. The actual problem analyzed, shown in Fig. 16, consists of a small panel mounted on a two-dimensional panel holder and exposed to Mach 6.57 flow. The purpose of such a test would be to obtain experimental data for code validation. The panel is simply supported at the lateral edges. This constraint restricts longitudinal thermal growth causing the panel to deflect convexly or concavely, depending on whether the constraint is on the inner or outer surface, respectively. Either deflection alters the aerodynamic flow field causing shock and expansion waves as shown schematically in Fig. 17. The thermal deformations and increased surface temperature both alter the aerodynamic heating distribution as shown in Fig. 18 for the convex panel. The increased wall temperature reduces the heating rate because of the reduced fluid thermal gradient at the wall. However, the heating rate and pressures are increased where the flow is compressed through shock waves (forward part of the panel, See Fig. 17) and decreased where the flow passes through expansion waves (aft part of the panel). The resulting thermal stress distributions are shown in Fig. 19 for the convexly distorted panel.

An experimental heat transfer model representative of a cowl leading edge has also been analyzed³⁶ with LIFTS. The analysis is for a three inch diameter cylinder immersed in Mach 6.47 flow. The thickness of the cylinder makes the cylinder stiffer than a flight weight leading edge. The flow field analysis³⁶ is shown in Fig. 20 to compare well with the experimental results of Wieting³³. The resulting temperature and stress distributions are also given. In this case the thermal deformations are insignificant and do not effect the flow field, which is coupled to the thermal response of the cylinder³⁶.

The more severe condition of shock-on-lip could not be analyzed with the explicit Taylor-Galerkin algorithm because of the prohibitively small time step^{30,36}. The implicit algorithm in LARCNESS is being added to LIFTS as an alternative fluid module to eliminate this shortcoming. The pressure and heating rate distributions based on experimental data³⁵ were input to LIFTS and an integrated thermal-structural analysis performed on the actively cooled leading edge shown in Fig. 21. Thermal and structural results for shock-on-lip at a simulated Mach 16, 2000 psf dynamic pressure are given in Fig. 22 and 23, respectively. The leading edge is assumed to be made of copper. The copper exhibits thermal super conductivity at cryogenic temperatures³⁶. The radial thermal gradients at the impingement point (Fig. 22) of the supersonic jet results in acceptable circumferential stresses as shown in Fig. 23. However, the circumferential thermal gradient (approximately 700 °F) results in axial stresses that exceed the elastic limit of the material. An unexpected benefit of the nonlinear Taylor-Galerkin algorithm developed for the flow analysis is its capability for nonlinear structural analysis^{36,41,42}. Temperature dependent stress-strain relations and large deformations are accommodated by

updating the finite element matrices during each analysis iteration. A shortcoming of this approach is that rate dependent material effects, which are known to be important at high temperatures, are neglected. Research is currently underway to include such effects using unified viscoplastic theory⁴³.

Current research is focused on further improvements and evaluation of the various algorithms, turbulence models, chemical equilibrium, adaptive meshing for thermal and structural analysis, hierarchical methods, a posteriori error estimates, and extension to three dimensional for all disciplines.

Concluding Remarks

To meet the analysis requirements for hypersonic vehicles the NASA Langley Research Center is developing the Langley Integrated Fluid-Thermal-Structural (LIFTS) analyzer using finite element techniques. A general automated unstructured gridding is used to discretize the aerodynamic and coolant flow field and the structure for the thermal and structural analyses. Currently a single nonlinear finite element algorithm provides the solution for the environment, loads and response for all three disciplines. The flow field computational domain is adaptively refined based on flow field gradients to minimize grid points and increase accuracy.

The historical development, status, and plans of the integrated fluid-thermal-structural methodology in LIFTS are discussed. The development was initiated in the mid 1970's with the development of a finite element thermal analyzer equivalent to standard finite difference thermal analyzers and interfaced with a structural analyzer. The next step was the development of an integrated thermal-structural analyzer which uses hierarchical elements with nodeless variables. Current research is focused on the development of efficient algorithms and adaptive refinement techniques. The algorithm, developed for the inherently nonlinear fluid equations, has led to unexpected benefits in the solution of nonlinear thermal and structural behavior.

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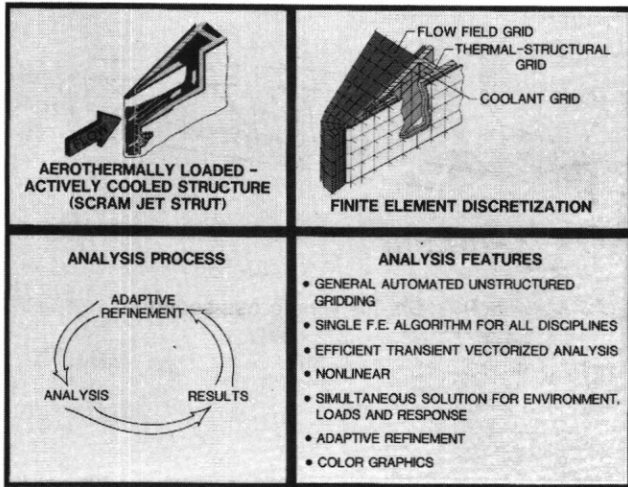


Fig. 1 Illustration of Langley Integrated Fluid-Thermal-Structural Finite Element Analysis Procedure.

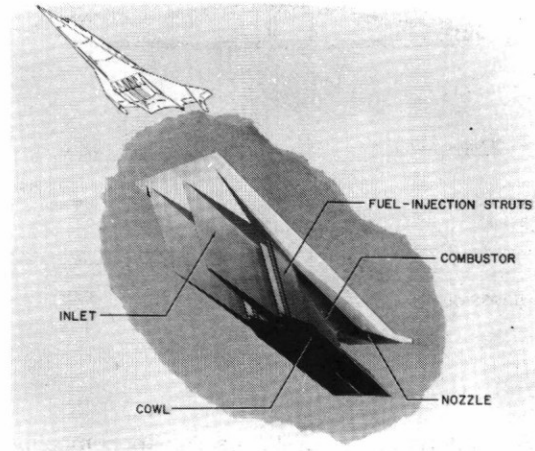
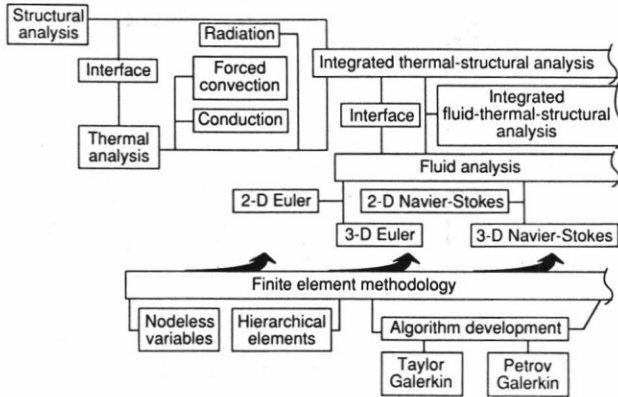


Fig. 3 Airframe-integrated supersonic combustion ramjet.



(a) Past and Present

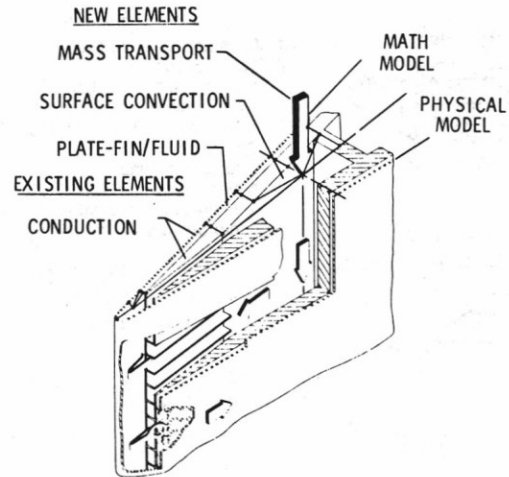
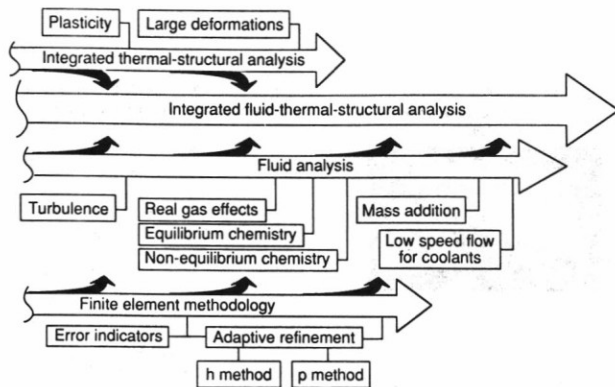


Fig. 4 Thermal element development for actively cooled structure.



(b) Future

Fig. 2 Past, Present, and Future development of integrated finite element methods in LIFTS.

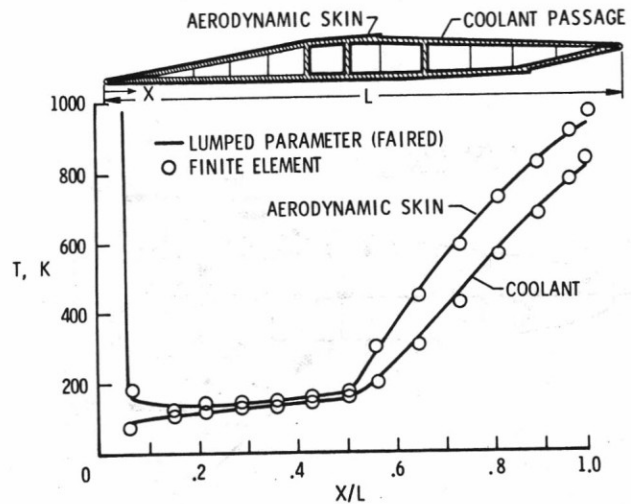


Fig. 5 Comparison of finite element and finite difference techniques in predicting thermal response of an actively cooled strut.

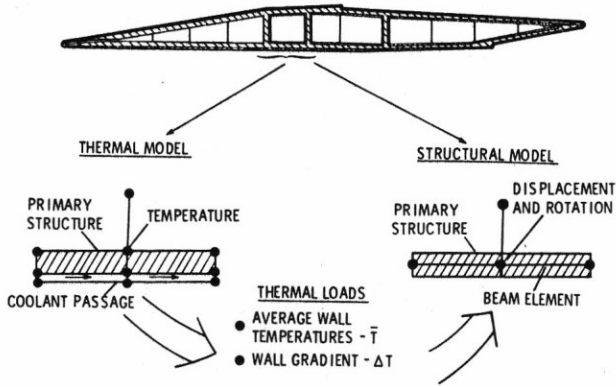


Fig. 6 Thermal-structural finite element compatibility.

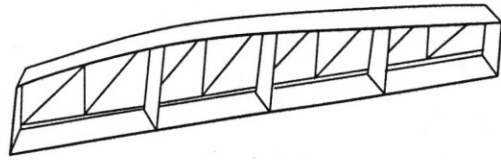


Fig. 9 Shuttle wing cross-section.

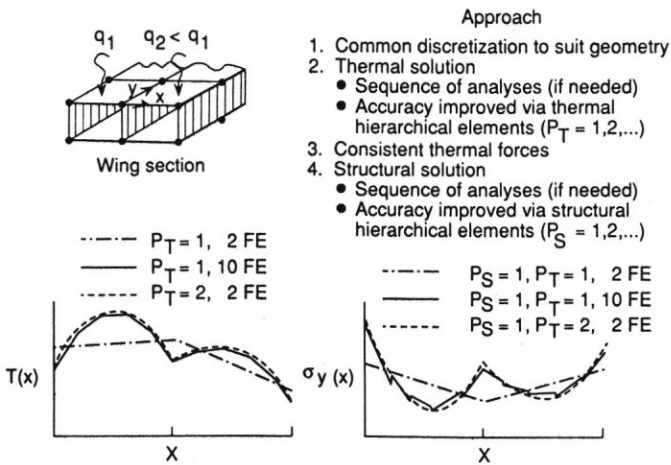


Fig. 7 Integrated thermal structural analysis with hierarchical thermal elements with nodeless variables.

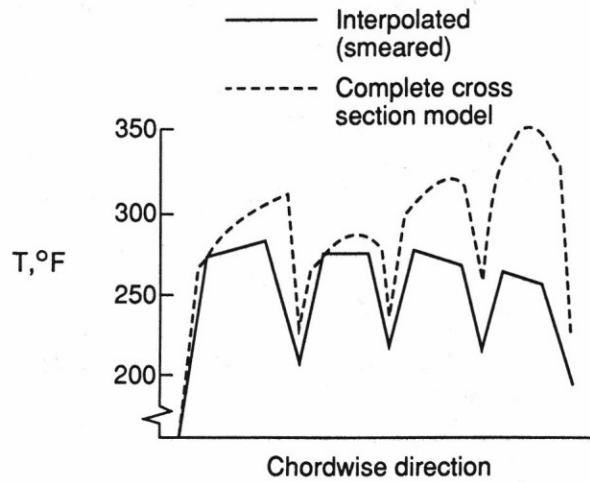


Fig. 10 Comparison of interpolated temperatures with detailed cross section temperatures.

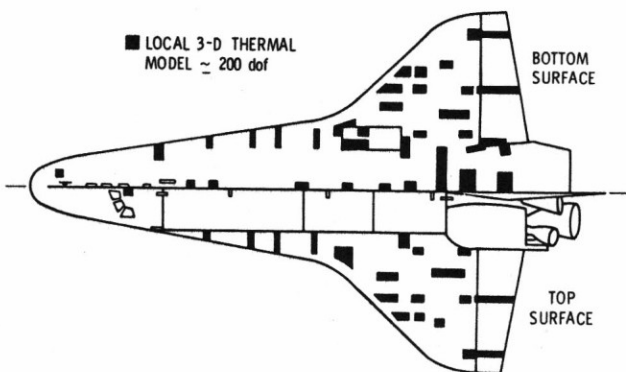


Fig. 8 Three dimensional plug model location for shuttle thermal analysis.

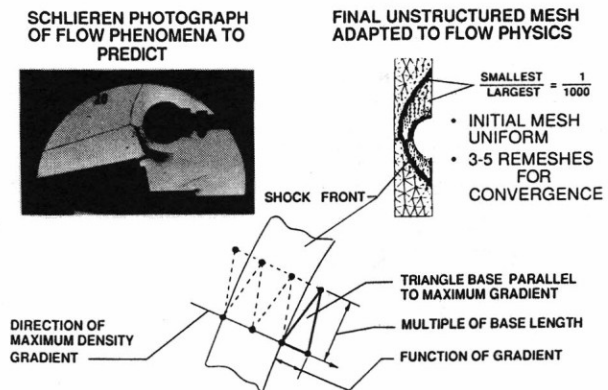


Fig. 11 Adaptive unstructured remeshing scheme.

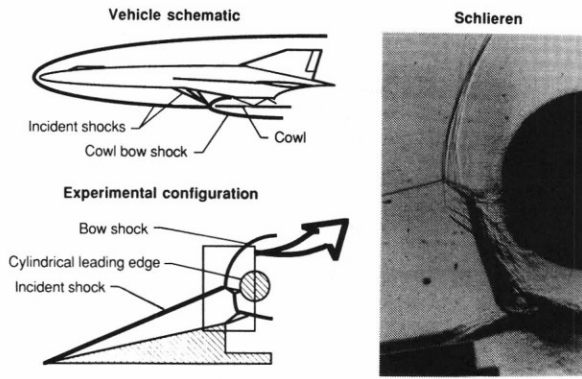


Fig. 12 Shock-on-lip interference phenomena.

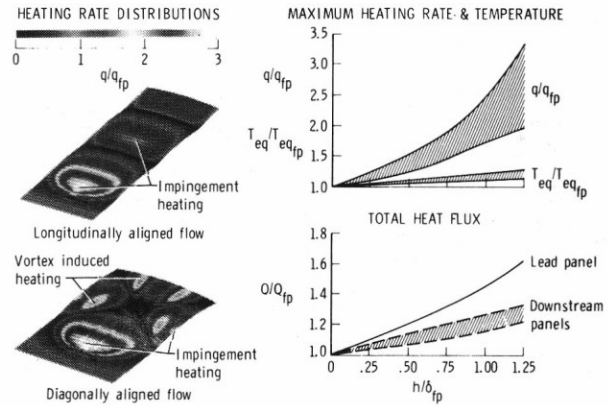


Fig. 15 Navier-Stokes analysis of thermally bowed TPS showing augmented thermal loads.

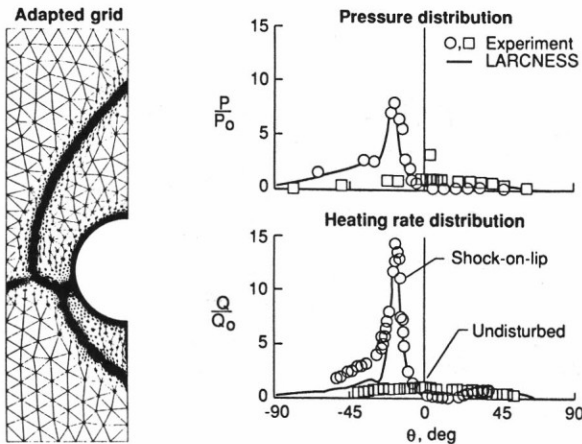


Fig. 13 LARCNESS adapted grid and comparison with experiment.

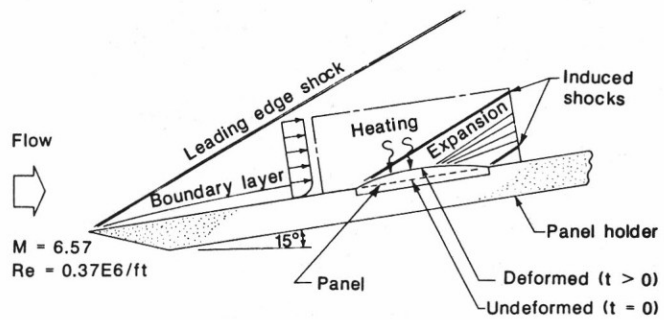


Fig. 16 Schematic of aerodynamically heated panel thermally bowing into flow field.

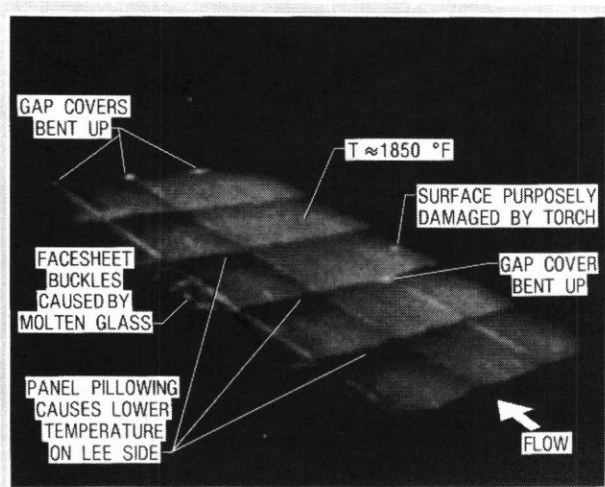


Fig. 14 Metallic TPS deformed during aerothermal exposure at Mach 7.

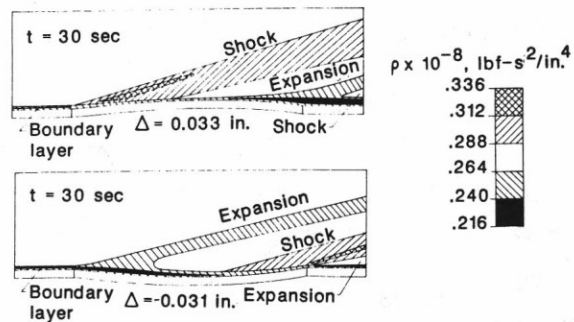


Fig. 17 Schematic showing interaction of convex and concave panel deflections on aerodynamic flow.

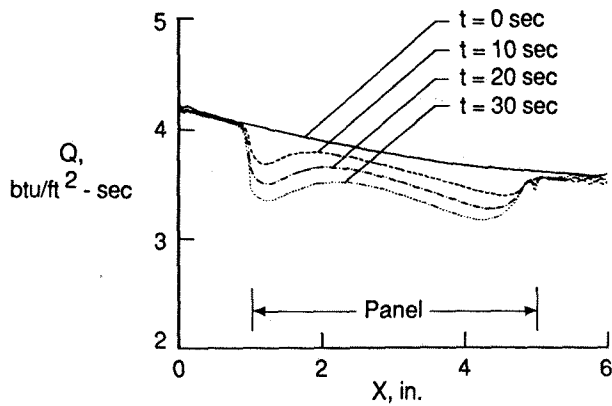


Fig. 18 Effect of surface temperature distribution and deformations on the panel heating rate distribution.

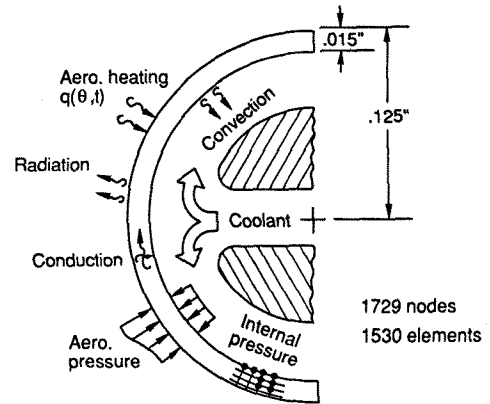


Fig. 21 Schematic of actively cooled cylindrical leading edge.

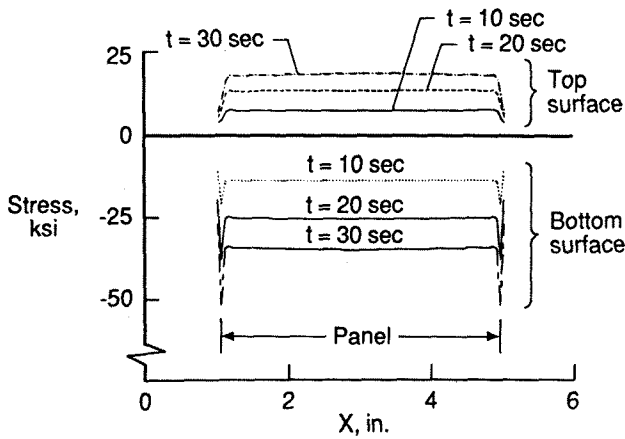


Fig. 19 Panel thermal stress distributions corresponding to heating rates at different times.

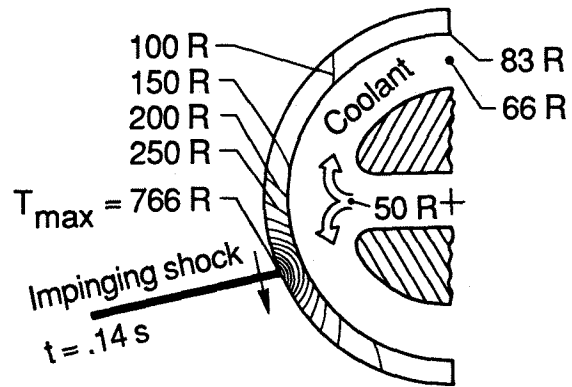


Fig. 22 Thermal response of leading edge with shock-on-lip.

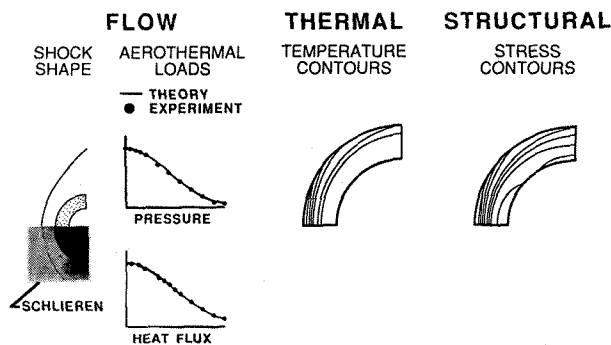


Fig. 20 Flow-thermal-structural behavior of a cylindrical leading edge as predicted by LIFTS.

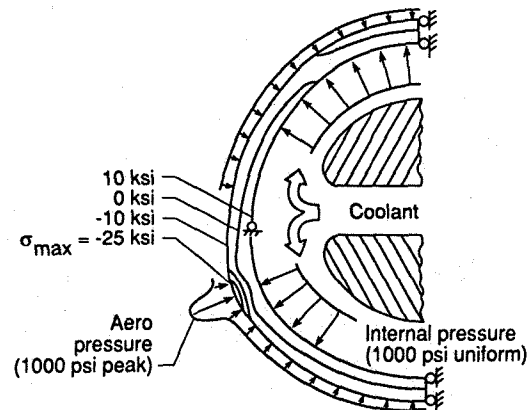


Fig. 23 Circumferential thermal and mechanical stress distribution in leading edge.